

# To Tell the Truth: Imperfect Information and Optimal Pollution Control

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# Introduction

- Self-interested agents will systematically deceive the regulatory authority when asked to reveal their information.
- A necessary condition for designing an optimal pollution control plan is knowledge of both the damages resulting from pollution and the costs of reducing pollution.
- This paper will focus on the policy implications of an asymmetry between the regulatory authority and polluters concerning information about clean-up costs.
- He examines the incentives of firms to deceive the regulatory authority when confronted with two standard pollution control policies, and then propose a new scheme

- There is only one form of pollution, and
- All waste discharged has the same impact on the environment
- These expected damages are denoted by  $D(X)$ , where  $X$  is the total amount of pollution discharged.  $D'(X) > 0$  and that  $D''(X) > 0$
- There are  $n$  firms, and  $C_j(X_j)$  describes the cost of clean-up for firm  $j$ , where  $X_j$  is its output of pollution.
- When there is no government controls:  
 $C_j(X_j) = 0$ ,  $C_j'(X_j) < 0$ ,  $C_j''(X_j) > 0$
- At the minimum,  $C'(X) = C_j'(X_j)$  for all  $j$ . Since  $C_j''(X_j) > 0$  for all  $j$ , it follows that  $C''(X) > 0$ .

- The government's objective is to minimize the sum of clean-up costs and expected damages from pollution,  $D(\sum_j X_j) + \sum_j C_j(X_j)$ .
- Therefore the optimal  $X_j$  :

$$D'(\sum_j X_j) + C' \sum_j (X_j) = 0.$$

- the government knows nothing about the aggregate clean-up cost function,  $C(X)$
- Suppose the government regulators ask all firms to report their pollution control cost functions. The function reported by firm  $j$  is denoted by  $\hat{C}_j(\cdot)$ , for all  $j$ .

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$$\hat{C}(X) \equiv \min_{\{X_j\}} \sum_{j=1}^n \hat{C}_j(X_j), \text{ subject to } \sum_{j=1}^n X_j = X.$$

- **PURE LICENSING:** Let  $L$  be the number of licences issued, and  $p$  be the market price of a licence. It is assumed that the market for licences is competitive
- **Firm  $j$  seeks to minimize:**

$$\min_{\{X_j, L_j\}} C_j(X_j) + pL_j, \text{ subject to } X_j \leq L_j.$$

- Thus, an optimum requires  $L_j = X_j$ . The first-order condition for a cost minimum is:  $C'_j(X_j) + p = 0$
- The market demand for licences: Let  $L_j$  be the  $j$ th firm's demand for licences, and let  $L^d = \sum_j L_j^d$ . If the price of a licence is  $p$ , each firm chooses  $X_j$  so that  $-C'_j(X_j) = p$  and  $L_j^d = X_j$
- When  $L$  licences are issued, the aggregate level of pollution will be  $L$ , since in equilibrium  $\sum_{j=1}^{j=n} X_j = L_d = L$ .

- The socially optimal  $L$ , is given by the first-order condition,  $D'(L) + C'(L) = 0$ .
- Each firm  $j$  will desire to report a  $\hat{C}_j(\cdot)$  which will minimize  $p$
- Therefore, the government will gain no useful information by asking firms to report their costs of clean-up when firms believe that the information will be used to set  $L$  in a pure licensing scheme

- The government regulators plan to set a charge of  $e$  per unit of pollution
- Each firm minimizes the sum of its clean-up costs and effluent fees,  $C_j(X_j) + eX_j$ .
- It does this by choosing  $X_j$  such that  $-C_j'(X_j) = e$ .
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The socially optimal  $e$ , which minimizes the sum of damages and clean-up costs, is given by the first-order condition

$$D'[X(e)] = -C'[X(e)] = e.$$

Suppose the government asks firms to report their pollution control cost functions, and firms believe that the government will set  $e$  such that

$$D'[X(e)] = -\hat{C}'[X(e)] = e.$$

- The firm would have been at least as well off by reporting a clean-up cost function with lower marginal costs for all levels of pollution output

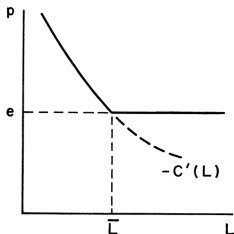
- The plan has two parameters:
- (i)  $L$  transferable licences are issued.
- (ii) A subsidy of  $e$  per licence in excess of emissions is paid to firms holding such licences
- firm  $j$  seeks to minimize the sum of treatment costs plus licence fees minus rebates or

$$C_j(X_j) - e(L_j - X_j) + pL_j = C_j(X_j) + (p - e)L_j + eX_j$$

subject to the constraint that emissions do not exceed licences, i.e.  $X_j \leq L_j$ .



- The government asks all firms to report their pollution control cost functions after announcing that it will set the parameters  $L$  and  $e$  so that  $DI(L) = -\widehat{C}'(L) = e$ .
- **Theorem.** Under the mixed effluent charge-licence plan, each firm's total costs are minimized when the government sets the socially optimal effluent subsidy and stock of licences
- Truth telling is a Nash equilibrium
- Given that no firm can do better than when everyone tells the truth, it may be reasonable for each firm to assume that all other firms are telling the truth.



- We might also expect that frequent changes in the tax rate or number of licences issued would imply heavy administrative and enforcement costs for the regulatory authority. Thus, a central desirable feature of the mixed effluent charge-licence plan is its ability to hit the right point once-and-for-all.